Optimization model to support decision making for silvopastoral systems in Uruguay

CLAIO 2024

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October 30, 2024



1 Introduction to Silvopastoral Systems

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- 2 Research Objectives
- 3 Methodology
- 4 Model Formulation
- 5 Results & Analysis
- 6 Conclusions

What are Silvopastoral Systems (SPP)?

- Agroforestry practice combining:
 - ForestryLivestock
 - Pastures
- Seeks to maximize economic & environmental benefits
- Typical cycle: 8-15 years



Figure: Silvopastoral system in Tacuarembo, Uruguay. Photo by J. L. Dutra

Rows and alleys



Rows and alleys(cont.)

- 1 Determine optimal spatial arrangement of trees
- 2 Calculate maximum livestock load per year
- 3 Optimize profits for both forestry and livestock
- 4 Consider terrain features and component interactions

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Forestation treatment

- Number of rows
- Distance between rows
- Distance between trees
- Corridor width
- Forest harvest year
- 3 Maximum livestock load per year

- Mathematical programming approach
- Mixed-integer nonlinear programming (MINLP) model
- Linearization technique used
- Validation through base case and sensitivity analysis

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Actual data from an Uruguayan livestock farm

Model

Production area: 150 m × 200 m

- Treatment chosen:
 - 4 rows
 - 6 meters between rows
 - 3.5 meters between trees
 - 30 meters corridor width
- Optimal forest harvest year: 13
- Total profit: \$14,402 USD
- Average annual profit: \$1,108 USD

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Base Case Results (cont.)

Figure: Inverse relationship observed (wood volume increases, livestock capacity decreases)

Forest harvest year Impact:

- 1 Year 13 maximizes both:
 - Total profit
 - Average annual profit
- 2 Factors:
 - Wood quality increase

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- Price changes
- Discount factor

Responsive to:

- Wood growth factors
- Tree density
- Dry matter availability
- Lower density \rightarrow higher individual tree growth

Trade-off between quantity and quality

- **1** Forestry more profitable than livestock
- 2 Optimal balance needed for system sustainability
- 3 Model accurately represents real-world trade-offs

- 4 Year 13 optimal for wood cutting
- 5 Consistent treatment choice across scenarios

- Decision support tool for producers
- 2 Scientific approach to system optimization
- 3 Contribution to Uruguay's productive matrix

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- 4 Framework for future research
- 5 Promotes sustainable agriculture

- Improve component interaction modeling
- Include environmental factors
- Consider soil quality preservation
- 4 Develop more detailed shade functions

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5 Enhance tree growth relationships

Thank you for your attention!

