

TABLA DE DERIVADAS

| Funciones elementales | | Funciones compuestas | |
|-------------------------------------|---|-------------------------------------|---|
| Función $f(x)$ | Derivada $f'(x)$ | Función $f(u)$ con $u = u(x)$ | Derivada $f'(x) = f'(u) \cdot u'(x)$ |
| $f(x) = k$ | $f'(x) = 0$ | | |
| $f(x) = x$ | $f'(x) = 1$ | | |
| $f(x) = x^p \quad p \in \mathbb{R}$ | $f'(x) = px^{p-1}$ | $f(u) = u^p \quad p \in \mathbb{R}$ | $f'(u) = pu^{p-1}u'$ |
| $f(x) = \ln x$ | $f'(x) = \frac{1}{x}$ | $f(x) = \ln u$ | $f'(x) = \frac{u'}{u}$ |
| $f(x) = \log_a x$ | $f'(x) = \frac{1}{x \ln a}$ | $f(x) = \log_a u$ | $f'(x) = \frac{u'}{u \ln a}$ |
| $f(x) = e^x$ | $f'(x) = e^x$ | $f(u) = e^u$ | $f'(u) = e^u u'$ |
| $f(x) = a^x$ | $f'(x) = a^x \ln a$ | $f(u) = a^u$ | $f'(u) = a^u \ln a u'$ |
| $f(x) = g(x)^{h(x)}$ | $f'(x) = h(x) g(x)^{h(x)-1} g'(x) + g(x)^{h(x)} \ln g(x) h'(x)$ | | |
| $f(x) = \operatorname{sen} x$ | $f'(x) = \cos x$ | $f(x) = \operatorname{sen} u$ | $f'(x) = \cos u u'$ |
| $f(x) = \operatorname{cos} x$ | $f'(x) = -\operatorname{sen} x$ | $f(x) = \operatorname{cos} u$ | $f'(x) = -\operatorname{sen} u u'$ |
| $f(x) = \operatorname{tg} x$ | $f'(x) = \frac{1}{\cos^2 x} = 1 + \operatorname{tg}^2 x$ | $f(x) = \operatorname{tg} u$ | $f'(x) = \frac{u'}{\cos^2 u} = (1 + \operatorname{tg}^2 u) u'$ |
| $f(x) = \operatorname{arcsen} x$ | $f'(x) = \frac{1}{\sqrt{1-x^2}}$ | $f(x) = \operatorname{arcsen} u$ | $f'(x) = \frac{u'}{\sqrt{1-u^2}}$ |
| $f(x) = \operatorname{arccos} x$ | $f'(x) = \frac{-1}{\sqrt{1-x^2}}$ | $f(x) = \operatorname{arccos} u$ | $f'(x) = \frac{-u'}{\sqrt{1-u^2}}$ |
| $f(x) = \operatorname{arctg} x$ | $f'(x) = \frac{1}{1+x^2}$ | $f(x) = \operatorname{arctg} u$ | $f'(x) = \frac{u'}{1+u^2}$ |
| $f(x) = \operatorname{sh} x$ | $f'(x) = \operatorname{ch} x$ | $f(x) = \operatorname{sh} u$ | $f'(x) = \operatorname{ch} u u'$ |
| $f(x) = \operatorname{ch} x$ | $f'(x) = \operatorname{sh} x$ | $f(x) = \operatorname{ch} u$ | $f'(x) = \operatorname{sh} u u'$ |
| $f(x) = \operatorname{th} x$ | $f'(x) = \frac{1}{\operatorname{ch}^2 x} = 1 - \operatorname{th}^2 x$ | $f(x) = \operatorname{th} u$ | $f'(x) = \frac{u'}{\operatorname{ch}^2 u} = (1 - \operatorname{th}^2 u) u'$ |
| $f(x) = \operatorname{arg sh} x$ | $f'(x) = \frac{1}{\sqrt{1+x^2}}$ | $f(x) = \operatorname{arg sh} u$ | $f'(x) = \frac{u'}{\sqrt{1+u^2}}$ |
| $f(x) = \operatorname{arg ch} x$ | $f'(x) = \frac{1}{\sqrt{x^2-1}}$ | $f(x) = \operatorname{arg ch} u$ | $f'(x) = \frac{u'}{\sqrt{u^2-1}}$ |
| $f(x) = \operatorname{arg th} x$ | $f'(x) = \frac{1}{1-x^2}$ | $f(x) = \operatorname{arg th} u$ | $f'(x) = \frac{u'}{1-u^2}$ |